Ability Estimation in Computerized Adaptive Test using Mamdani Fuzzy Inference System

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Ability Estimation in Computerized Adaptive Test using Mamdani Fuzzy Inference System

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Abstract. Assessment is an activity to find out the learning outcomes of a course. Conventionally, assessment is done using a pencil and paper test. Along with the development of information and communication technology, assessment can be done computerized, known as Computer Based Test (CBT). The Computerized Adaptive Test (CAT) is one form of CBT where the items given are chosen based on the students' abilities. This research aims to design a system that can estimate the ability of students based on the parameters of the questions and answers given. The estimation method uses the Mamdani Fuzzy Inference System (MFIS). The input MFIS are a level of difficulty and discrimination of the questions, the probability of students being able to answer correctly and the student's answer, while the output is an ability estimated. Based on this fuzzy system output, the next item questions will be determined according to the ability of the students. 24 IF-THEN rules are used for fuzzy systems. CAT simulations are carried out for Linear Algebra Course. The type of question given is multiple choice. Giving items will be stopped if the value of the estimated ability of the students has not changed. From the simulations carried out, it was obtained that, for one topic, the ability of the student can be acquired with the number of questions as many as six questions. So that the CAT system can minimize the time of the exam, reduce the subjectivity of the assessment and can arrange for each student to get the questions according to his abilities.

1. Introduction

Assessment activity of learning outcomes in the cognitive/knowledge domain is usually done with objective and descriptions test techniques with various paper or also called a pencil and paper test. Along with the development of information and communication technology, the assessment of student learning outcomes can be done computerized (known as Computer Based Test/CBT). The use of CBT in examinations can reduce the subjectivity of lecturers in conducting assessments, is not affected by the condition of the lecturers (tired, unfocused) and certainly can reduce the use of paper (in accordance with environmentally friendly principles). At CBT it is possible to randomize questions between one student and another student. In the sense that every student is allowed to get a different sequence of questions. This can prevent students from collaborating in completing the exam. However, the form of an exam like this can cause an inaccuracy in giving questions and less efficient time between one student and another.

Computerized Adaptive Testing (CAT) is a test method for test participants that is managed based on the level of participants' abilities [1]. Based on that, the score of the assessment of each examinee will not be much different, both those with more and moderate abilities. This is because the system used in CAT is able to recognize the level of participants' abilities so that the questions given is a matter that

can be done by the participants. The design of the CAT as an instrument for evaluating learning outcomes has advantages including: (a) assisting lecturers in evaluating learning outcomes (reducing subjective elements, not affected by lecturers' condition/tired or out of focus); (b) in accordance with environmentally friendly principles because it reduces the use of paper in conventional examinations; (c) can be integrated with online learning (e-learning) so that it allows students to conduct self-assessment.

The main key to the CAT program is the computer's ability to provide the right questions "adaptively" according to the estimation of test takers' abilities. In general, the CAT system consists of five main amponents, namely [2, 3, 4]:

- calibrated item bank,
- 2. the starting point,
- 3. item selection rule,
- 4. scoring, and
- stopping rule.

Given 1 and 2, repeat 3 and 4 until 5 is satisfied.

At the stage of item selection, an algorithm is needed that can estimate the ability of the examinees so that the items to be issued are adjusted to the abilities of the participants. The classic method of knowing the level of participants' ability is to the Maximum Likelihood estimator (MLE) [5, 6]. Bayesian method used in [7, 8] to estimate participants' ability. In this research, estimation of participants' abilities will be carried out using fuzzy logic. In general, Fuzzy Logic Control (FLC) has four main parts as shown in Figure 1. The four parts have the following functions [9, 10]:

- 1. Fuzzifier functions to transform input signals that are crisp to the fuzzy set using the fuzzifier operator.
- 2. The Knowledge Base contain a database and basic rules that define fuzzy sets of input and output areas and arrange them in the control rules.
- 3. Decision Making is at the core of FLC which has the ability to be human in making decisions. Fuzzy set actions are inferred using fuzzy implications and fuzzy inference mechanisms.
- 4. Defuzzier functions to transform conclusions about fuzzy set actions into actual variable that are crisp by using defuzzier operators.

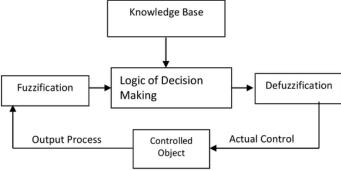


Figure 1. Fuzzy logic control

2. Method

In this research, the block diagram of the fuzzy logic system to estimate the ability of examinees as shown in Figure 2. There are 4 inputs to fuzzy system, namely:

- 1. Item difficulty level (b_i) , with 3 levels namely easy, medium and difficult.
- 2. question discrimination (a_i), with 2 levels namely satisfactory and good.
- 3. Probability of the examinees answer the question correctly (p_i) , calculated using Equation 1 [6].

$$\rho_i(\theta) = c_i + (1 - c_i) \frac{e^{1.7a_i(\theta - b_i)}}{1 + e^{1.7a_i(\theta - b_i)}} \quad i = 1, 2, 3, ..., n$$
 (1)

where,

 $p_i(\theta)$: the probability that the student has the ability θ to answer the item i correctly

 θ : student's ability estimate

 b_i : item difficulty level

ai: item discrimination

ci: guessing factor

n: the number of items

e: 2.718

The parameter c is worth 0.25 because there are only 4 possible answers on each questions (multiple choice questions). This input is divided into two categories namely minimum and maximum.

4. Participant's response or answer (r_i) , if the correct answer is worth 1, whereas if the wrong answer is 0

Input 1 and input 2 are the question parameters.

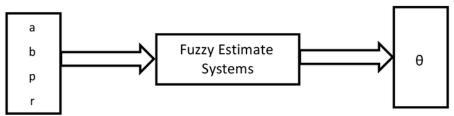


Figure 2. Block diagram of the fuzzy estimate system

Fuzzy system output is the estimated value of the participant's ability (θ) . This output is divided into 5 levels namely Very Low (VL), Low (L), Average (Av), Great (G) and Excellent (Ex). These five output levels adjust to the values in the student scoring system, which is from the highest value A to the lowest value E. While the values B_{5} and D are in the two values.

The membership functions of the four inputs and one output can be seen in Figure 3 to Figure 7.

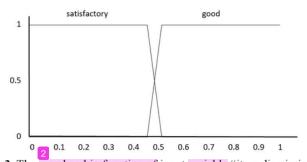


Figure 3. The membership function of input variable "item discrimination"

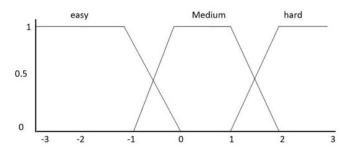


Figure 4. The membership function of input variable "item difficulty level"

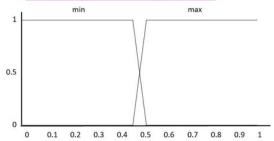


Figure 5. The membership function of input variable "Probability"

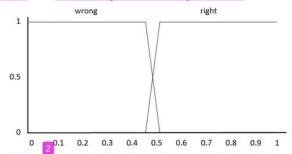


Figure 6. The membership function of input variable "participants' response"

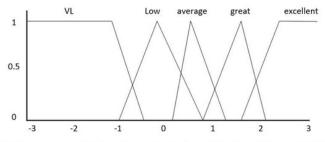


Figure 7. The membership function of output variable "participants' abilities level"

Based on the above input-output fuzzy system, fuzzy system rules are then compiled to estimate the ability of the examinees. There are 24 fuzzy IF ... THEN ... rules, as summarized in Table 1. The value 1 in Table 1 shows input or output at that level. For example, rule number 1 states that,

IF discrimination is satisfactory AND difficulty is easy AND probability is minimum AND response is wrong THEN ability is very low.

The logic that underlies rule number 1 is that if an exam participant is given an easy question and he/she answers incorrectly, the level of ability is very low. Other fuzzy rules are built based on relevant logic.

Fuzzy system designed using Mamdani fuzzy model with the defuzzification process using center of gravity defuzzyfier.

Table 1. Fuzzy system rules

| Rule | | Input | | | | | | | | | Output | | | |
|------|------------------------|-------|----------------|---|-------|--------------------|-----|--------------|---|--------------------|--------|----|---|----|
| No. | Discrimi nation (a) | | Difficulty (b) | | Proba | Probability (p) | | Response (r) | | Ability (θ) | | | | |
| | | | | | | | | | | | | | | |
| | G | S | Н | M | Е | Max | Min | R | W | VL | L | Av | G | Ex |
| 1 | | 1 | | | 1 | | 1 | | 1 | 1 | | | | |
| 2 | | 1 | | | 1 | | 1 | 1 | | | 1 | | | |
| 3 | | 1 | | | 1 | 1 | | | 1 | 1 | | | | |
| 4 | | 1 | | | 1 | 1 | | 1 | | | | 1 | | |
| 5 | | 1 | | 1 | | | 1 | | 1 | | 1 | | | |
| 6 | | 1 | | 1 | | | 1 | 1 | | | | 1 | | |
| 7 | | 1 | | 1 | | 1 | | | 1 | | 1 | | | |
| 8 | | 1 | | 1 | | 1 | | 1 | | | | | 1 | |
| 9 | | 1 | 1 | | | | 1 | | 1 | | | 1 | | |
| 10 | | 1 | 1 | | | | 1 | 1 | | | | | 1 | |
| 11 | | 1 | 1 | | | 1 | | | 1 | | | 1 | | |
| 12 | | 1 | 1 | | | 1 | | 1 | | | | | | 1 |
| 13 | 1 | | | | 1 | | 1 | | 1 | | 1 | | | |
| 14 | 1 | | | | 1 | | 1 | 1 | | | | 1 | | |
| 15 | 1 | | | | 1 | 1 | | | 1 | 1 | | | | |
| 16 | 1 | | | | 1 | 1 | | 1 | | | | 1 | | |
| 17 | 1 | | | 1 | | | 1 | | 1 | | | 1 | | |
| 18 | 1 | | | 1 | | | 1 | 1 | | | | | 1 | |
| 19 | 1 | | | 1 | | 1 | | | 1 | | 1 | | | |
| 20 | 1 | | | 1 | | 1 | | 1 | | | | | | 1 |
| 21 | 1 | | 1 | | | | 1 | | 1 | | | 1 | | |
| 22 | 1 | | 1 | | | | 1 | 1 | | | | | | 1 |
| 23 | 1 | | 1 | | | 1 | | | 1 | | | 1 | | |
| 24 | 1 | | 1 | | | 1 | | 1 | | | | | | 1 |

3. Result and Discussion

The design of fuzzy system to estimate the ability of examinees, then simulated using system simulation software. For simulation purpose, we use the item bank for Linear Algebra Course. There are 177 multiple choice questions for six topics, namely vector, matrices concepts, matrices operation, determinant, inverse, and matrices applications.

We can see the results of this simulation to what extent the fuzzy system that is built can produce the expected output. As the first question, a question with a moderate level (Medium) is chosen and the probability of correct answer = 0.5. Table 2 to Table 4 shows the different scenario of simulation for the Vector topic.

The first scenario is if the answer continues right (see Table 2). In this case, the difficulty level of the question will increase (medium to hard level) along with the increase in the estimation of participants'

abilities (θ) . The test for this subject will stop at the fourth question, because at that time the estimated ability value (θ) has not changed anymore.

Table 2. Simulation results of vector topics if response continues right

| Stage | Level | No. of Question | a | b | p | r | С | θ | Δθ |
|-------|-------|--------------------|-----|---------|--------|---|------|--------|--------|
| 1 | M | 16 | 0,8 | -0,4055 | 0,5 | 1 | 0,25 | 1,874 | |
| 2 | H | 28 | 0,1 | 1,7346 | 0,6294 | 1 | 0,25 | 2,207 | 0,333 |
| 3 | H | 29 | 0,1 | 2,9444 | 0,6015 | 1 | 0,25 | 2,4589 | 0,2519 |
| 4 | H | 30 | 0,1 | 2,9444 | 0,6095 | 1 | 0,25 | 2,4589 | 0 |

The second scenario is if the participant's answer is wrong. In Table 3 can be seen that the level of difficulty of the question will go down (from medium to easy) along with the decrease in the estimation of the ability of the examinee (θ) . The test will stop at the third question, because the value of (θ) no longer changes.

Table 3. Simulation results of vector topics if response continues wrong

| Stage | Level | No. of Question | a | b | p | r | С | θ | Δθ |
|-------|-------|--------------------|-----|---------|--------|---|------|---------|---------|
| 1 | M | 16 | 0,8 | -0,4055 | 0,5 | 0 | 0,25 | -1,0786 | |
| 2 | E | 12 | 0,5 | -1,0986 | 0,6282 | 0 | 0,25 | -1,8853 | -0,8067 |
| 3 | E | 8 | 0,3 | -1,7346 | 0,6105 | 0 | 0,25 | -1,8853 | 0 |

The third scenario is if the participants' answers are right and wrong alternately (see Table 4). This results in the estimation of the ability (θ) to change continuously or $\Delta\theta$ will not reach zero. Likewise the level of difficulty of the problem will be fluctuating (medium - hard - medium). In this third case, the procedure for stopping the exam is if the number of questions has reached 6 items.

For other topics (namely matrices concepts, matrices operation, determinant, inverse, and matrices applications), we obtain the simulation result that tends to be the same as the results on the vector topic.

Table 4. Simulation results of vector topics if response right and wrong alternately

| Stage | Level | No. of Ouestion | a | b | p | r | С | θ | Δθ |
|-------|-------|--------------------|-----|---------|--------|---|------|--------|---------|
| 1 | M | 16 | 0,8 | -0,4055 | 0,5 | 1 | 0,25 | 2,0819 | |
| 2 | H | 28 | 0,1 | 1,7346 | 0,6360 | 0 | 0,25 | 0,2873 | -1,7946 |
| 3 | M | 21 | 0,8 | 0,4055 | 0,5949 | 1 | 0,25 | 2,4589 | 2,1716 |
| 4 | H | 29 | 0,1 | 2,9444 | 0,6095 | 0 | 0,25 | 0,6657 | -1,7932 |
| 5 | M | 26 | 0,3 | 0,619 | 0,6294 | 1 | 0,25 | 1,5 | 0,8343 |
| 6 | H | 30 | 0,1 | 2,9444 | 0,5791 | 0 | 0,25 | 0,6657 | -0,8343 |

4. Conculusion

It has been successfully designed a Computerized Adaptive Test (CAT) with an estimation of participants' abilities using the Mamdani Fuzzy Inference System. The simulation process was carried out for Linear Algebra Courses with 6 topics, namely vector, matrices concepts, matrices operation, determinant, inverse, and matrices applications. The simulation results show that for each topic at most 6 questions are delivered and the system has been able to know the participants' abilities.

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